

## GIG 9.0 Guidance Notes on Cone Penetration Testing

### Part 2: Correlation of Geotechnical Parameters with CPT Raw Data and Application

#### 1. Undrained Shear Strength

Correlations of the undrained shear strength  $S_u$  with the cone resistance  $q_c$  have been adopted for many years. The undrained shear strength  $S_u$  of a fine-grained cohesive soil depends on some factors like material composition, anisotropy, strain rates, stress and stress history amongst others.

There are three approaches for the interpretation of undrained shear strength with CPT as below:

- Estimation of  $S_u$  by cone resistance  $q_c$
- Estimation of  $S_u$  by total cone resistance  $q_t$
- Estimation of  $S_u$  by effective cone resistance  $q_e$   
( i.e.,  $q_e = q_t - u_2$ )
- Estimation of  $S_u$  by excessive pore pressure

The cone factor  $N_k$  is derived from  $q_c$  is based on theoretical approaches, and after modification and improvement, the cone factor  $N_{kt}$  derived from  $q_t$  using empirical correlation becomes more commonly adopted than other estimations. The total (Corrected) cone resistance  $q_t$  and the vertical overburden pressure ( $\sigma_{vo}$ ) is correlated with an average undrained shear strength,  $S_u$ , by the following equation:

$$S_u = (q_t - \sigma_{vo}) / N_{kt} \\ = q_n / N_{kt}$$

where

$S_u$  is the inferred undrained shear strength

$q_t$  is the measured cone resistance

$N_{kt}$  is an empirical bearing capacity or cone factor relating  $q_t$  to strength

$\sigma_{vo}$  is the total overburden pressure

$q_n$  is net cone resistance that is corrected cone resistance minus vertical stress

The undrained shear strength of a soil stratum could be calculated from the known  $q_t$  valve measured at a depth below the seabed. Since the unconfined compressive strength (UCS) of the soil could be obtained with soil sample from laboratory test, the correlated value of  $S_u$  from CPT can be verified by the UCS from laboratory for the cohesive soil. The equation is used to calculate  $S_u$  of the clayey stratum with the following equation:

$$S_u = \text{UCS} / 2 \text{ ----- Equation 1}$$

For the corrected  $q_t$  of a soil layer is 1,000 KPa at depth of 17m below seabed, the undrained shear strength can be calculated as follow:

$$S_u = (q_t - \sigma_{vo}) / N_{kt} = (1000 - 17 \times 17) / 14 = 50.7 \text{ KPa} \\ \text{UCS} = 2 \times 50.7 = 101.4 \text{ KPa.}$$

Aas et al. (1986) correlated  $N_{kt}$  with the average shear strengths from triaxial laboratory tests in compression, extension and direct shear tests. However, the cone factor must be determined empirically, from correlations based on previous investigations in the same material or correlated with insitu vane tests. Experience has shown that an  $N_{kt}$  factor in the range 10 to 18 may normally be used to give an initial estimate of shear strength (Lunne et al. (1997). Typically,  $N_{kt}$  is averaged with 14, and it tends to increase with increasing plasticity and decrease with increasing soil sensitivity. This correlation should only be confined in Zone 1, 2, 3, 4 and 9 in the Normalised Soil Behaviour Type (SBTn) chart for the clay-like soil. Studies show that the value of the factor varies from 4 to greater than 30 due to some factors including sensitivity, plasticity, fissuring and possibly consolidation. Lunne et al., 1997 also showed that  $N_{kt}$  varies with pore pressure ratio  $B_q$ , where  $N_{kt}$  decreases and  $B_q$  increases, when  $B_q \sim 1.0$  (i.e., sensitive clay),  $N_{kt}$  can be as low as 6.

The correlation between  $S_u$  and  $N_{kt}$  are generally conducted at specific sites in Hong Kong. The Figure 1 shows that the  $N_{kt}$  values vary from 17 to 23.5 for firm and stiff to soft clay for Chek Lap Kok Airport Project since 1997.

Summary of design parameters (Greiner-Maunsell, 1991a)				
Typical Index Properties and Recommended Design Parameters	Upper Soft Clay	Stiff Clay	Firm-to-Stiff Clay	Lower Sand
Unit Weight ( $Mg/m^3$ )	1.45	1.90	1.85	2.00
Void Ratio, $e_c$	2.00	(2)	1.03	0.65
Maximum Past Pressure, $P_p^{(1)}$	$P_p = 4.5 + 7z$	N.A.	$P_p = 55 + 15z$	N.A.
Compression Index, $C_c$	1.20	(2)	0.42	N.A.
Recompression Index, $C_{cr}$	0.10	(2)	0.085	0.03
Coeff. of Consolidation, $c_v$ ( $m^2/year$ )	1.3	(2)	2.2	N.A.
Coeff. of Reconsolidation, $c_{vr}$ ( $m^2/year$ )	20	(2)	15	N.A.
Undrained Shear Strength $N_k = q_{net}/S_u$ ( $kN/m^2$ )	$N_k = 23.5$	$N_k = 21.25^{(1)}$	$N_k = 17$	N.A.
Secondary Compression $C_{\alpha}$	N.A.	0.3%	1.5%	N.A.

Fig 1. The designed  $N_k$  (i.e.,  $N_{kt}$ ) values adopted by Greiner after the series of field tests and studies in Chek Lap Kok Airport Site.

It should be noted that the  $N_{kt}$  values will not be applicable as  $q_c$  may not be measured accurately in very soft clay at shallow and intermittent depth. In addition, the use of subtraction type of CPT cone may not be appropriate for  $q_c$  measurement in very soft clay as compared with the cone type equipped with separated sensors for  $q_c$  and  $f_s$  measurements. A more appropriate method for correlation of  $S_u$  in very soft to soft soils is adopted to measure the difference of pore pressure with the following equations:

$$S_{ru} = \frac{\Delta u}{N_{\Delta u}} \quad \text{----- Equation 2}$$

$$N_{\Delta u} = B_q N_{kt} \quad \text{----- Equation 3}$$

where

$$\Delta u = u_2 - u_0$$

$N_{\Delta u}$  = Cone factor for excessive pore pressure.

$N_{\Delta u}$  generally varies from 4 to 10. However, in lack of reliable data, the upper bound value is recommended to be selected. In order to enhance the performance of the correlation, the cone filter should be free from clogging and the cone should be fully saturated without air bubble entrapped.

The local professionals seldom adopt this method to correlate with  $S_u$  particularly in very soft clay stratum. Therefore, there are limited relevant data obtained. One of the large infrastructures in Tung Chung had acquired the test data as shown in Figure 2. Most of the  $N_{\Delta u}$  results are between 8 and 13, and the average value is around 10.

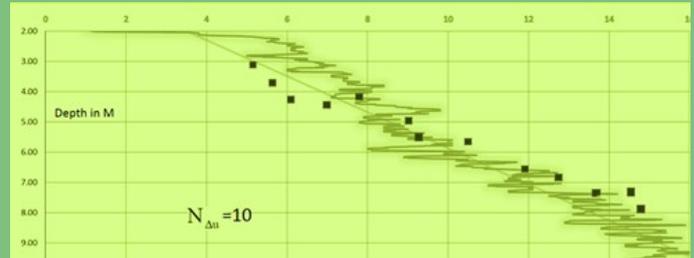


Fig. 2 Correlation of vane shear tests and excessive pore pressure with  $N_{\Delta u}$  of 10.

### 1.1 Remoulded Undrained Shear Strengths

The remoulded shear strength of soil can be obtained from vane shear test. After completion of the peak shear strength test, the vane is rotated with 12 complete revolutions to shear the soil. Then pause for 5 minutes before commencement of vane test again to find the remoulded shear strength (Refer Figure 3 for details). Alternatively, the sleeve friction from the CPT testing can be used to derive the peak remoulded shear strength of clay. The following equation expresses the measured sleeve friction resistance ( $f_s$ ) as the remoulded shear strength of clay:

$$f_s \approx S_u (\text{remoulded})$$

This equation shows the lower bound value in assessing the  $S_u$  profile, and it is applicable for the SBTn in Zone 1, 2, 3, 4 and 9. The sleeve friction must be measured accurately as the remoulded  $S_u$  may be as low as in between 5 to 10 KPa range.

The peak resistance strength for soil is dominantly measured from the  $q_c$  of CPT whereas the residual or the remoulded shear strength is dominantly measured with  $f_s$ . The correlation test results for  $S_u$  and remoulded  $S_u$  from an overseas site are manifested in Figure 4.



Fig. 3 Peak and remoulded shear strength from vane shear test

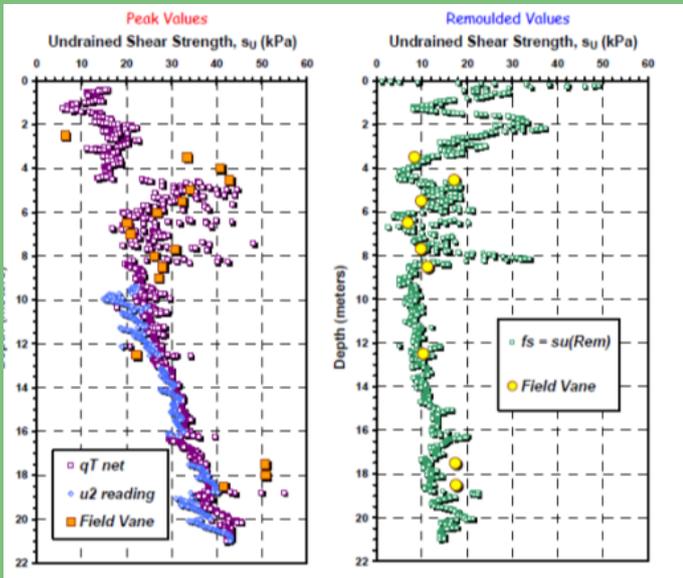


Fig. 4 Typical correlation of CPT ( $N_{ki}$  of 15 and  $N_{AU}$  of 10) with peak and remoulded shear strengths of field vane shear test

## 2. Standard Penetration Test

Standard Penetration Test (SPT) is one of the several obsolete and imperfect tests remain in common use in many parts of the world. Mayne et al (2009) correctly questions the false sense of reality in the geotechnical engineer's ability to assess each of the soil parameters from a single N-value. The geotechnical engineers should progressively abandon this crude and unreliable in-situ testing method. However, the simple operation with low cost reasonably explains that why the SPT method is used continuously in most parts of the world.

The CPT cone resistance  $q_c$  can directly be correlated to SPT N-value according to the following general linear equation:

$$q_c = n N, \text{ where } q_c \text{ in MPa}$$

The study from Schmertmann (1970) found that the constant, n value ranges from 0.2 for silt to sand, and to 2 for sand to sand gravel. It depends on the soil type and condition as reported from some previous studies. The study for hydraulic fill in Tung Chung by CEDD (GEO Report 42, 1977) found that the relationship between  $q_c$  and N values for the overall soil profile, the marine deposit and the sandfill as shown in Figure 5. Hence, it is therefore important that the correlation for  $q_c$  and N values should be conducted specifically for large local projects.

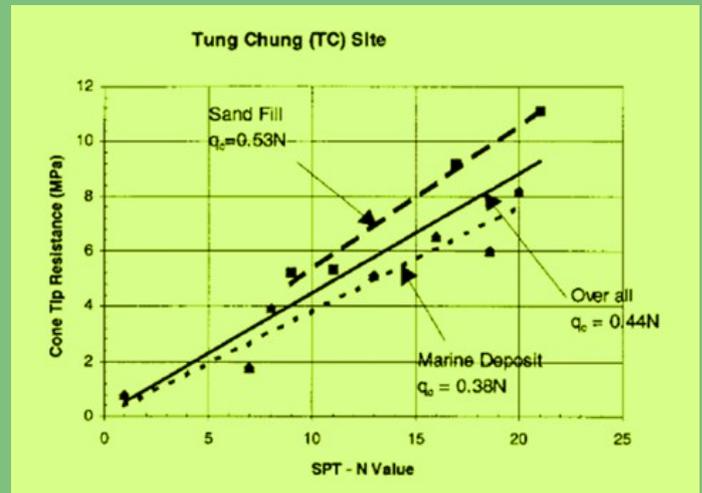


Fig. 5 Correlation of  $q_c$  and SPT N value

Many studies have been conducted to correlate SPT N values and  $q_c$ . Robertson and Campanella (1983) reviewed the correlations and presented the ratio of  $(q_c / \text{Pa}) / N_{60}$  with the mean particle size of soils ( $D_{50}$ ) as shown in the Figure 6. The range of the soil  $D_{50}$  is confined from 0.001mm to 1mm.

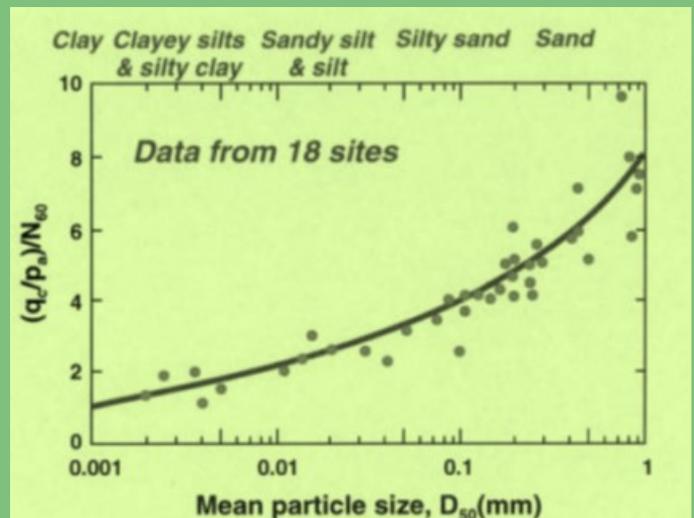


Fig.6 Correlation of modified SPT N values and  $D_{50}$  of soils

The other studies have correlated the SPT N values with CPT and fine content for sandy soils which are shown in Figure 7.

As series of laboratory tests should be conducted to get the mean grain sizes of  $D_{50}$  and fine contents for soils, it makes the correlation of SPT N values with these two parameters becomes impracticable. Besides, the correlation of CPT data with soil  $D_{50}$  is limited between 0.01 mm and 1 mm. The CPT has a trend of increasing friction ratio with increasing fines and decreasing grain size.

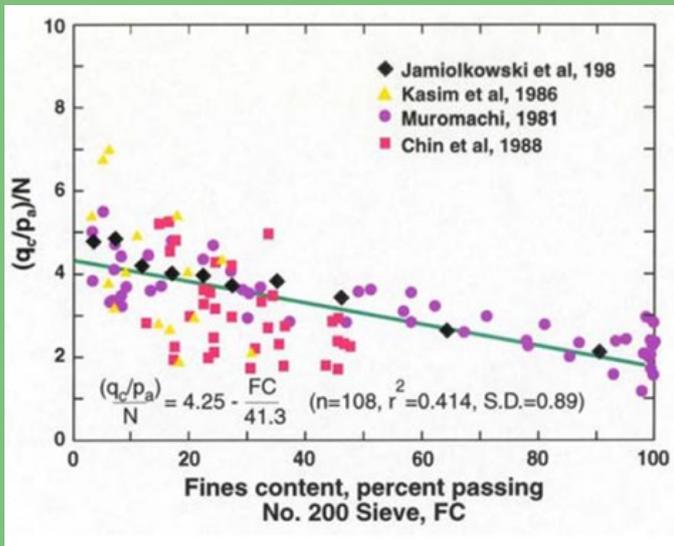


Fig. 7 Correlation of  $(q_c / p_a) / N$  values and fines content for soils

Robertson et al. (1986) suggested to use the non-normalized CPT chart for  $(q_c / p_a) / N_{60}$  ratios of each soil behaviour type zone. The suggested  $(q_c / p_a) / N_{60}$  ratio for each soil behaviour type is given in Table 1. For fine grained soft soils, the correlations should be applied to total cone resistance,  $q_t$ . Note that in sandy soils,  $q_c = q_t$ .

Zone	Soil Behavior Type (SBT)	$\frac{(q_c / p_a)}{N_{60}}$
1	Sensitive fine grained	2.0
2	Organic soils – clay	1.0
3	Clays: clay to silty clay	1.5
4	Silt mixtures: clayey silt & silty clay	2.0
5	Sand mixtures: silty sand to sandy silt	3.0
6	Sands: clean sands to silty sands	5.0
7	Dense sand to gravelly sand	6.0
8	Very stiff sand to clayey sand*	5.0
9	Very stiff fine-grained*	1.0

Table 1. Relationship of CN and SBT Zone No.

Jefferies and Davies (1993) suggested that the most reliable method to convert the CPT cone resistance,  $q_t$ , to an equivalent SPT N value at 60% energy,  $N_{60}$ . With the soil behaviour type index,  $I_c$ , it can be combined with the CPT- SPT ratios to give the following simple relationship:

$$C_N = (q_t / p_a) / N_{60} = 8.5 [1 - (I_c / 4.6)] \text{ ----- Equation 4}$$

It should be noted that the  $N_{60}$  can be calculated based on  $I_c$  and  $q_t$  where  $N_{60}$  is defined in the following equation (Skempton 1985):

$$N_{60} = (ER N C_B C_S C_R) / 60 \text{ ----- Equation 5}$$

Where ER is the efficiency ratio of the free-fall energy for different types of SPT hammers (Refer to Table 2), and it lies between 40 and 73 by ignoring the % in the above equation. The ERs for different types of hammers are different. Some of the publications show that the ER for a fully automatic hammer may go as high as 85%.

	North America	South America	Middle East	United Kingdom	Japan	Hong Kong
Borehole Diameter (mm)		South America	100 to 150	152 to 375	65 to 110	89 to 140
Hammer Mechanism	Slip-rope, safety	Slip-rope	Automatic trip	Automatic trip	Slip-rope	Automatic trip
Average Rod Energy Efficiency(%)	45 to 60	45 to 50		73	65	?

Table 2. Summary for Energy Efficiencies for Different Types of SPT Hammers

The Constants  $C_B$ ,  $C_S$  and  $C_R$  expressed in Table 3 are adjustment factors related to the borehole diameter, the sampling method adopted and the depth of SPT testing being conducted.

Factor	Equipment Variables	Value
Borehole diameter factor, $C_B$	2.5 - 4.5 in (65 - 115 mm)	1.00
	6 in (150 mm)	1.05
	8 in (200 mm)	1.15
Sampling method factor, $C_S$	Standard sampler	1.00
	Sampler without liner	1.20
Rod length factor, $C_R$	10 - 13 ft (3 - 4 m)	0.75
	13 - 20 ft (4 - 6 m)	0.85
	20 - 30 ft (6 - 10 m)	0.95
	> 30 ft (> 10 m)	1.00

Table 3. Correction Factors for SPT Equipment and Operation

According to the  $N_{60}$  equation from Jefferies and Davies (1993) used to correlate the soil behaviour type  $I_c$ , the ER (Energy Efficiency Ratio) for different types of SPT hammers should be known for calculation of  $N_{60}$ . However, we do not know how the authors built up the equation correctly with different ER values of different types of SPT hammers. Refer Table 3 for details.

Despite the auto-trip SPT hammers is commonly used in Hong Kong for years, it has not been calibrated in terms of the hammer energy efficiency since 1997. GEO conducted the energy efficiency test in that year. It was reported (GEO Technical Report No, 2/97, 1997) that the ER values were pin between 29% and 43%. In view of the comparably lower values of the ER found, it was concluded that further study should be conducted to find out the discrepancy. Similar ER tests were conducted by Yang W. W. (2016), and he got the ER results between

33% and 80% with the mean value greater than 60%. Phillip Chung (2018) manifested at the HKIE Geotechnical Conference in 2018 that the average ER test result from GEO's study was found to be 68%. purpose, and further studies will be continued. It is recommended that Equation 4 delivered by Jefferies and Davis (1993) for correlation of SPT  $N_{60}$  should only be adopted in lack of reliable information and related field data from reasonable sources in your projects. Alternatively, the correlated values should be used conservatively with a higher safety factor.

### 3. Horizontal Coefficient of Consolidation ( $C_h$ )

For CPT carried out with piezocones, dissipation test can be performed to find the dissipation of any excess pore pressure recorded against time as presented in Figure 8. The rate of dissipation depends upon the coefficient of consolidation, which in turn, depends on the compressibility and permeability of the soil.

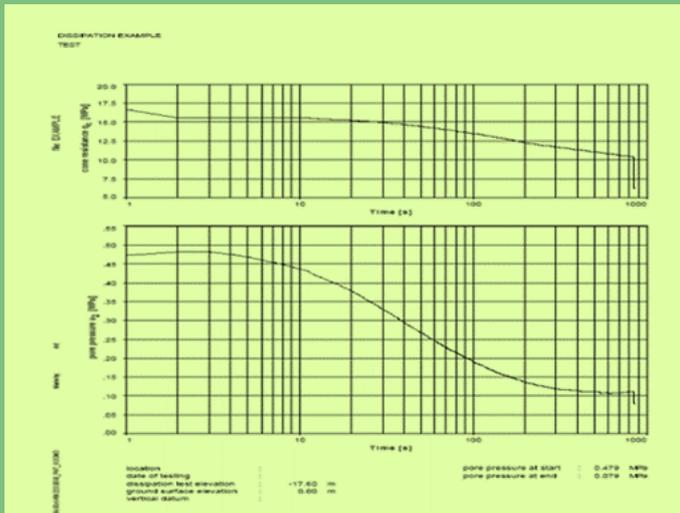


Fig 8. Plot for Dissipation Test Report

$$U = \frac{U_t - U_o}{U_i - U_o} \times 100\% \quad \text{Equation 6}$$

where

- $U_t$  = pore pressure at time  $t$
- $U_o$  = equilibrium pore pressure *in-situ*
- $U_i$  = pore pressure at start of dissipation test

Superimposing the Teh and Houlsby theoretical curve for dissipation over the actual curve,  $T^*$  (modified time factor) can be estimated as well as the value of  $t$ . An example is given in Figure 9 for ease of reference.

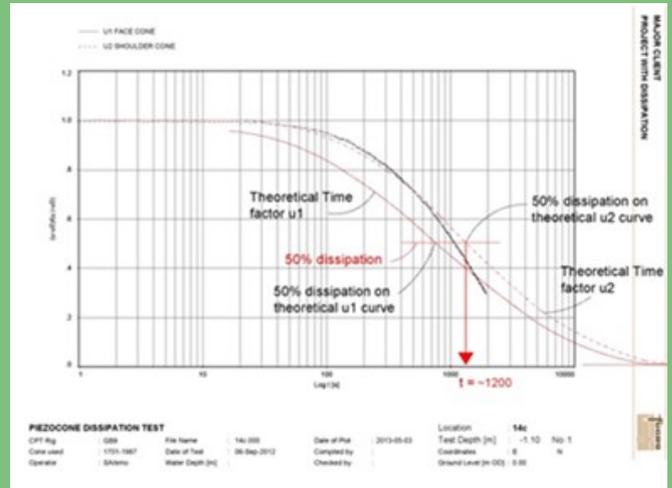


Fig 9. Dissipation Test for Determining  $t_{50}$

From the value of the modified time factor  $T^*$  it is possible to determine  $C_h$  from the following formula.

$$T^* = C_h \cdot t / r^2 \cdot I_R^{0.5} \quad \text{Equation 7}$$

where

- $T^*$  = Modified time factor
- $t$  = Actual time
- $r$  = Radius of CPT probe
- $I_R$  = Rigidity index =  $G / S_u$ . (Refer to Section 3.3)
- $C_h$  = Coefficient of consolidation in horizontal direction

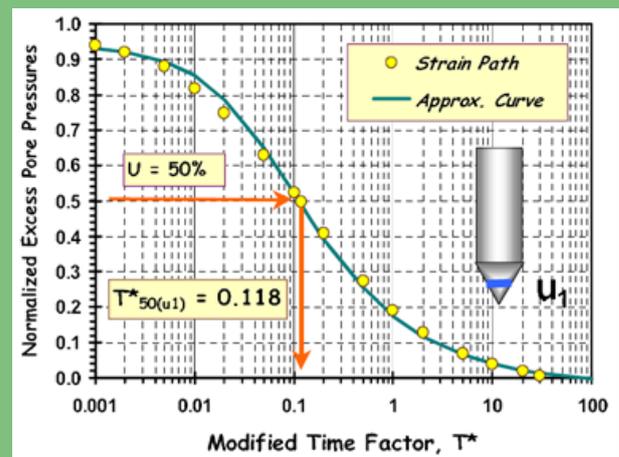


Fig 10A. Modified Time Factor for Monotonic Dissipation Test for Determining  $T_{50}$  for U1 Filter

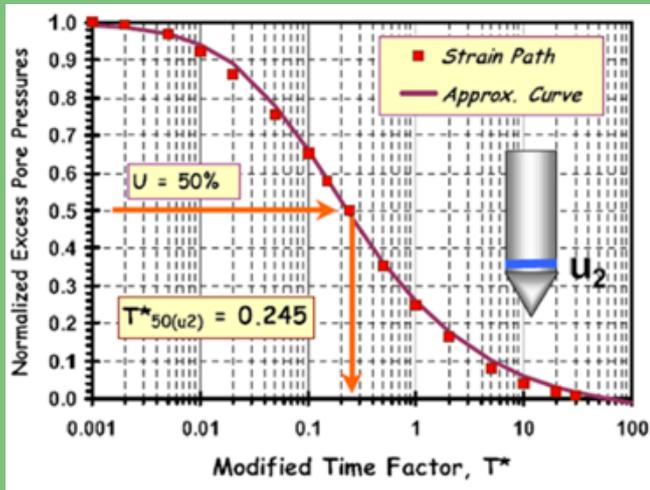


Fig 10B. Modified Time Factor for Monotonic Dissipation Test for Determining T50 for U<sub>2</sub> Filter

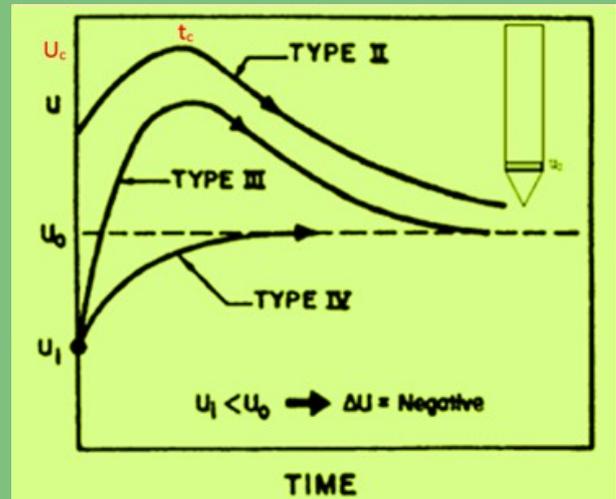


Fig.11C Type II to IV of Dilatory Dissipation

### 3.1 Types of Dissipation Tests

When cone penetration is halted, the induced excess pore pressure will dissipate until it reaches the hydrostatic pore pressure. A typical dissipation record shows the magnitudes of pore-water pressures monotonically decreasing with time from the initial reading. Refer to Figure 11A for details. It is similar to the behaviour of the one-dimensional consolidation test. The behaviour observed in normally to lightly overconsolidated clays when the cone filter is respectively located on the cone face ( $u_1$ ), behind the shoulder ( $u_2$ ), or behind the friction sleeve ( $u_3$ ). However, the behaviour observed in heavily overconsolidated clays is different for  $u_1$  but the different responses for  $u_2$  and  $u_3$  filters will be described under Section 4.3.

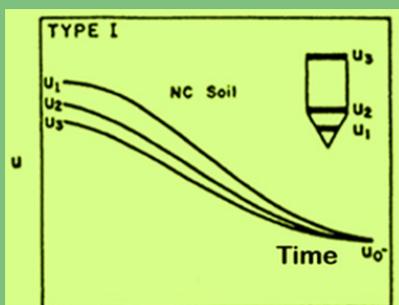


Fig.11A Type I of Monotonic Dissipation Curves

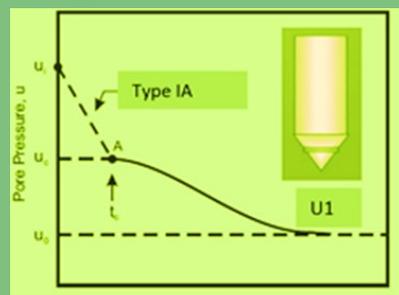


Fig.11B Type IA of Monotonic Dissipation Curves

### 3.2 Monotonic Dissipation (Type I and IA)

For Type 1 dissipation, the  $u_1$ ,  $u_2$  and  $u_3$  piezocone filters always decay with time in a monotonic characteristic pattern (i.e., pore pressure decreases with time) for normally to lightly overconsolidated soils. If 50% of the normalized pore pressure is adopted, the equation is expressed as below:

$$C_h = T_{50}^* r^2 I_R^{0.5} / t_{50} \text{ ----- Equation 8}$$

where

$T_{50}^*$  = Modified time factor at 50% of the normalized pore pressure

$t_{50}$  = Time of dissipation at 50% of the normalized pore pressure

$I_R$  = Rigidity index for soil

A typical calculation of  $C_h$  for Type I dissipation, the monotonic (standard) dissipation is shown in the Figure 12 and the following calculation method:

$u_0$  = Hydrostatic pressure = 128.76KPa

$u_i$  = Initial Pore water pressure = 579.6KPa

Dissipated pressure at 50%  
=  $(128.76 + 579.6) / 2 = 354.18$

$T_{50}^*$  = 0.245 for  $u_2$  filter cone = 354.18KPa

$r = 1.785\text{cm}$  for  $10\text{cm}^2$  cone

$(t_{50})^{0.5} = 0.584$

$t_{50} = 0.34\text{min}$

$I_R = 150$  (Assumed)

$C_h = 0.245 \times 1.785^2 \times (150)^{0.5} / 0.34$

=  $28.12 \text{ cm}^2/\text{min}$

=  $1.47 \times 10^3 \text{ m}^2/\text{yr}$

It should be noted that a smaller cone, 10cm<sup>2</sup> cone, is used for the test, it will give you a shorter time of t<sub>50</sub> when compared with the 15 cm<sup>2</sup> cone.

For Type1A dissipation, it should note that u<sub>1</sub> will exhibit a sudden drop of the initial pore pressure due to halt of penetration of the cone with unloading of cone. It is therefore important that the CPT rod should be locked during the dissipation test to avoid the sudden drop of pore pressure. The phenomenon is common for u<sub>1</sub> cone filter, but it is insignificant for the u<sub>2</sub> and u<sub>3</sub> filters. For calculation of C<sub>h</sub> based on pore pressure dissipation can be considered that the time t<sub>c</sub> (Refer to Fig. 11B) to be the initial time of dissipation and u<sub>c</sub> be the maximum pore pressure. The normalized excessive pore pressure for dissipation should be plot against either the log time scale or the square root of time and to get the new 50% of the excessive pore pressure dissipation, t<sub>50</sub>, from the graph. The C<sub>h</sub> can be calculated using the above equation.

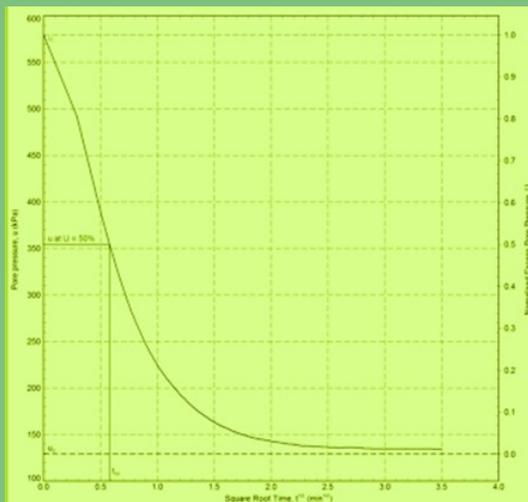


Fig. 12 Plot for Pore Pressure and Square Root Time for Monotonic Dissipation

### 3.3 Rigidity Index

The evaluation of rigidity index has long been considered problematic by interpretation of dissipation tests. The main difficulty in evaluating shear modulus is the variance of shear modulus with shear strain. Figure 13A illustrates shear modulus decreases with increase in shear strain. The initial shear modulus, G<sub>max</sub> shown in Figure 13B typically represents the maximum tangential modulus at very low strains, while a secant modulus is used for larger strain levels and shear modulus decreases with increasing strain level. As a compromise, G<sub>50</sub> suggested by Konrad & Law (1987) and Schnaid et al., (1997) is the shear modulus 50% of the mobilized strength, and it represents the average response of the soil around an advancing cone. Therefore, G<sub>50</sub> is considered appropriate to be adopted for calculation of I<sub>R</sub>.

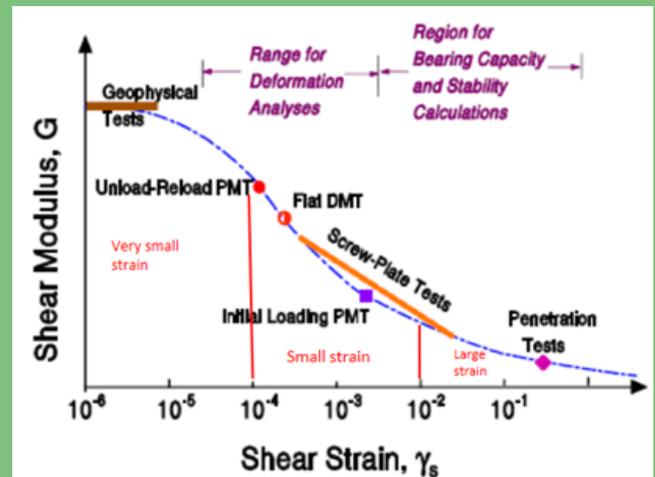


Fig. 13A Modulus Reduction Curve with Strain

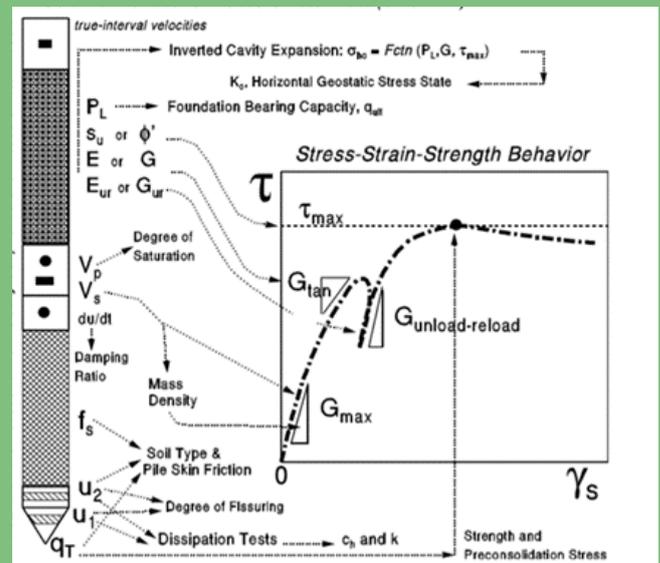


Fig. 13B Graph for Stress-Strain-Strength Behaviour Illustrates Different Shear Modulus from the Hybrid Tests of A Prospective Seismic Piezocone Pressuremeter

Keaveny and Mitchell (1986) proposed an empirical approach relating the rigidity index to the overconsolidation ratio (OCR) and clay plasticity index (PI). The methodology was based on results from triaxial CAUC test data on various clays where the I<sub>R</sub> (i.e., I<sub>R50</sub> = 50% of mobilized strength) was defined using G<sub>50</sub> = E<sub>50</sub> / 3. The developed correlation can be expressed as:

$$I_{R50} \approx \frac{\exp\left(\frac{137 - PI}{23}\right)}{1 + \ln\left[1 + \frac{(OCR - 1)^{3.2}}{26}\right]^{0.8}} \quad \text{----- Equation 9}$$

Figure 14 shows the relationship between the rigidity index, OCR, and PI based on Ko-consolidated triaxial compression.

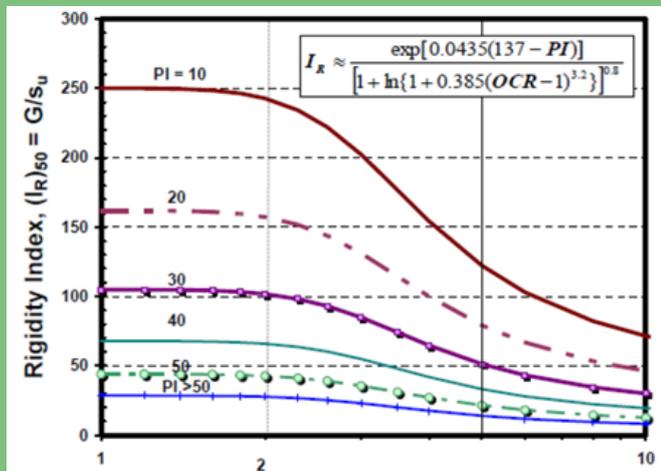


Fig. 14 Estimation of Undrained Rigidity Index of Soil from OCR and Plastic Index

The  $I_R$  varies from 20 for very highly plastic soils to 250 for low plastic soil. The maximum ratio of  $I_R^{0.5}$  for the former to the latter one is 3.54, and it is generally less than half of one order of magnitude for calculating the  $C_h$ . In consideration of the difficulties in determination of  $C_h$  accurately, it is acceptable that accuracy in the estimate of the coefficient of consolidation varies within one order of magnitude (Robertson 2015).

### 3.4 Dilatory Dissipation (Type II and III)

In many overconsolidated and fissured materials, a dissipation test may first show an increase in pore pressure with time after a halt of penetration. Then it reaches a peak value, and decreases subsequently in pore pressure with time to hydrostatic pressure. This type of pore pressure response as shown in Figure 11C is termed dilatory dissipation. The dilatory response is observed for  $u_2$  and  $u_3$  filter elements during piezocone dissipation tests as well as during installation of driven piles in fine-grained soils.

Compression-induced pore pressures from increasing normal stresses are always positive; however, shear-induced pore-water pressure may be either positive (contractive) or negative (dilatant). Under the cone tip, the shear stress component can be derived from stress path analysis, which always has positive values (Chen and Mayne 1994); additionally, the magnitude of the normal-induced response is often much larger than that of the shear-induced response under the cone tip. However, along the shaft, the normal-induced and shear-induced components can be comparable in magnitude. While the normal component will always remain positive, the shear-induced component can be positive at low overconsolidation ratios (OCRs) or negative at high OCRs. The dilative dissipation curve will occur if the compression-induced pore pressure is smaller than the shear-induced pore pressure during the dissipation test.

#### 3.4.1 Curve Fitting Method

Burns and Mayne (1998) used a model based on cavity expansion and critical-state soil mechanics theories to derive the results by a rigorous mathematical method. The solution process requires a computer program and iteration to obtain a good fit of the measured dissipation curve. During the fitting process both the horizontal coefficient of consolidation ( $C_h$ ) and the rigidity index ( $I_R$ ) are varied, which may be problematic and lacking a physical basis. It is not hereby to describe the method in detail due to the short cut purpose of this paper for quick application.

#### 3.4.2 Logarithmic and Square Root of Time Methods

To account for the dilatory response, an empirical offset method was suggested by Sully and Campanella (1994) whereby the curves were shifted to the maximum value of measured pore pressure and then subjected to the monotonic decay solution.

#### Logarithm of Time Plot

For the  $u_2$  filter, the maximum pore pressure,  $u_c$ , is taken as the peak value that occurs during the post-penetration increase and the time  $t_c$  at which this peak occurs is taken as the zero time of the dissipation record and all other times adjusted accordingly.

#### Square Root of Time Plot

The square root time plot is the most commonly used method for the dilatory dissipation. By means of extrapolating the portion of the straight line of the curve towards the ordinate to get the new value of the initial pore pressure  $u_c$ , the  $C_h$  can be calculated using the monotonic equation 8. The following typical calculation is illustrated with the plot in Figure 15:

$u_0 = 73.48\text{KPa}$   
 $u_i = 240\text{KPa}$   
 $u_c = 277\text{KPa}$  (Max. pore pressure from extrapolating line to Y axis)  
 For 50% of dissipation of the excessive pore pressure,  
 $u_{50} = (277 + 73.48) / 2 = 175.24\text{KPa}$   
 For 10 cm<sup>2</sup> cone with filter at shoulder ( $u_2$  type)  
 $T_{50}^* = 0.245$   
 $r = 1.785\text{cm}$   
 $t_{50} = 43.27\text{min}$   
 $I_R = 120$  (Assumed)

$$C_h = \frac{(T_{50}^*)r^2\sqrt{I_R}}{t_{50}} \text{----- Equation 9}$$

$$\begin{aligned} C_h &= 0.245 \times 1.785^2 \times (120)^{0.5} / 43.27 \\ &= 0.198 \text{ cm}^2/\text{min} \\ &= 10.3 \text{ m}^2/\text{yr} \end{aligned}$$

The advantage of the root-time method is that  $C_h$  can be calculated from the 50% pore pressure reduction if shorter dissipation period is used in the field and measured data for longer period is unavailable.

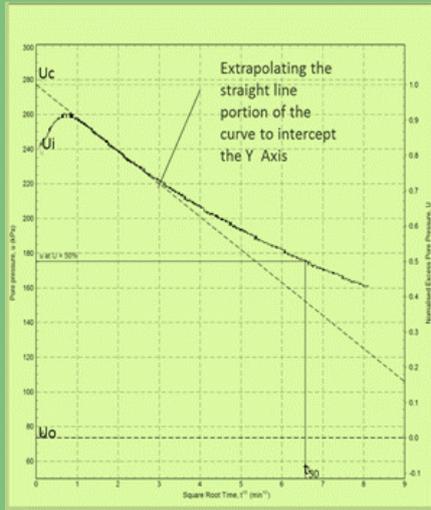


Fig. 15 Dilatory Dissipation Plot with Square Root Time Method

### 3.4.3 An Empirical Equation for Correcting $T_{50}$ To $T_{50m}$

The corrected value of  $t_{50m}$  can be used with existing methods of test interpretation to evaluate the field value of  $C_h$ . Chen et al, (2012) proposed  $C_h$  calculation for dilatory (Non-standard) dissipation based on the numerical results. The following empirical equation is proposed to correct  $t_{50}$ :

$$t_{50m} = \frac{t_{50}}{1 + 18.5 \left( \frac{t_{u\max}}{t_{50}} \right)^{0.67} \left( \frac{I_r}{200} \right)^{0.3}} \quad \text{----- Equation 10}$$

where

$t_{50m}$  = Corrected time for 50% excess pore pressure dissipation.

$t_{50}$  = Time difference between the maximum and 50% of the maximum excess pore pressure (Refer to Figure 16).

$t_{u\max}$  = Time for the measured excess pore pressure to reach its maximum value.

$I_r = I_R$  = Rigidity index

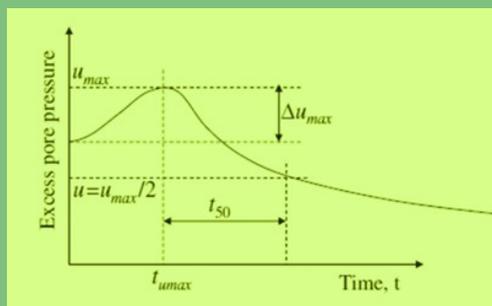


Fig. 16 Plot for  $t_{u\max}$  and  $t_{50}$  for A Dilatory Dissipation Curve

The corrected time  $t_{50m}$  can be used to replace  $t_{50}$  in the equation proposed by Teh and Houlsby (1991) for standard dissipation curve to calculate directly the value of  $C_h$  with the following equation.

$$C_h = \frac{T^* r^2 (I_r)^{0.5}}{t_{50m}} \quad \text{----- Equation 11}$$

If  $u_2$  filter is used, the equation becomes

$$C_h = \frac{0.245 r^2 (I_r)^{0.5}}{t_{50m}} \quad \text{----- Equation 12}$$

Despite the non-standard dissipation curves,  $C_h$  values evaluated by the proposed method are 2.6 to 8.8 times larger than those obtained without the  $t_{50}$  correction. However, the authors (Chai et al., 2021) concluded that values of  $C_h$  evaluated from the proposed method is more representative of the “true” or field values of the horizontal coefficient of consolidation than those evaluated using alternative methods.

### 3.4.4 Dilatory Dissipation (Type IV)

Type IV dilatory dissipation curves manifest that the initial pore pressure is negative, and it rises to the hydrostatic pore pressure but without reaching the peak pore pressure during the dissipation test. It can be considered that it is an inverse of the monotonic dissipation, and it can be treated as the standard dissipation type for calculation of the  $C_h$ .

## 4. Application of CPT in Deep Compaction Work

There are currently three popular deep compaction techniques to densify granular soil, namely, dynamic compaction, resonance compaction and vibroflotation (I.e., vibrocompaction). Vibroflotation is the most widely used deep compaction technique in Hong Kong attributed to many successful projects during the years. It is a process to “float” the soils by vibration to enable them to become arranged in a denser state.

### 4.1 Compactibility for Sandfill and CPT

Grain shape and particle size distribution play an important role in deep compaction. The silt fraction in sandy deposits should be less than 7% (Some researchers suggest the range to be between 7% and 10%) and the uniformity coefficient should be in the range from 2.2 to 6.8. Brown (1997) suggested that the granulometric curves as shown in Figure 17 with the suitability zones for vibroflotation. The soil granulometry indicates that the sandy deposit is ideally compactable in zone B and compactable in zone C.

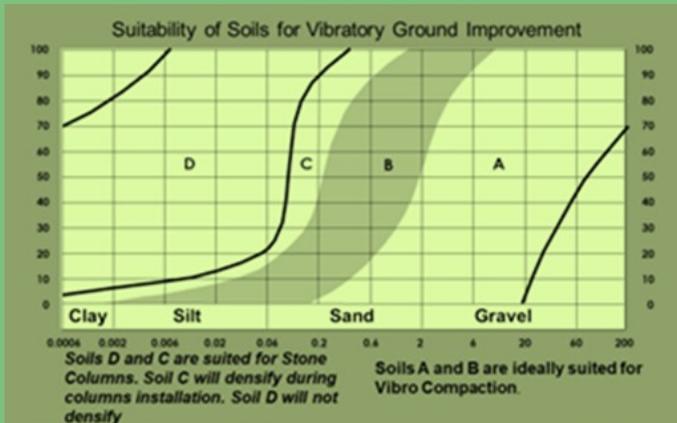


Fig. 17 Compactibility of Soil and Grain Size Distribution

In addition to the particle size distribution for soil, the increase of fines (i.e., soil particle can pass through the Sieve No 200, and the diameter of soil particles smaller than 0.074mm) will potentially inhibits the densification of soil. Figure 17 shows the broadly accepted range of grading suitable for vibroflotation. The fines content can also be exhibited in term of friction ratio on the SBT chart of  $q_c$  or  $q_t$  versus friction ratio.

Massarsch (1994) proposed an empirical relationship between cone resistance  $q_t$  and friction ratio as shown in Figure 18 to assess the compatibility of soils.

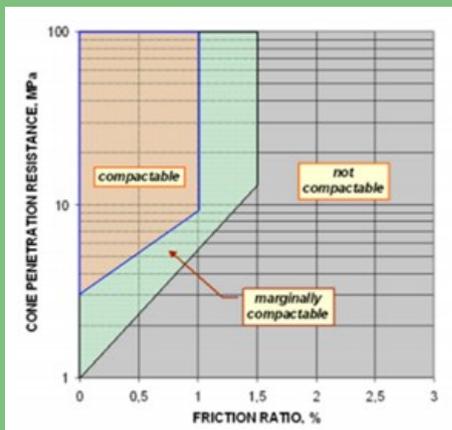


Fig.18 Classification of deep compaction and CPT Data

Soils with between 12 % silt and 30 % silt content and/or between 1 % and 5 % clay content are difficult to judge for their compatibility.

#### 4.2 CPT as Method of Acceptance Testing for Deep Compaction

CPT has become commonly adopted for quality control of the deep compaction because of the following reasons:

- It is fast and cost effective.
- Continuous profile with data can be acquired.
- The data obtained is reliable and repeatable.

- More parameters can be measured when compared with other in-situ tests. They include cone resistance, sleeve friction, pore water pressure and shear wave velocity if seismic cone is equipped.

It is difficult to obtain undisturbed samples of sands for laboratory testing to measure the in-situ densities directly from the deep compaction projects, CPT is then adopted to define the acceptance criteria for the reclamation projects in Hong Kong. One of the projects, the Disneyland site, specified that the  $q_c$  values should achieve the designated strengths along the depth profile as shown in Figure 19A.



Fig. 19A Typical Acceptance Criterion for Cone Resistance  $q_c$  at Penny Bay Project

For the Central Reclamation Project Phase III in Hong Kong, it is specified that the minimum  $q_c$  criterion based on effective stress of the soils along the depth profile should be achieved (Refer to Figure 19B). If the result of any post-compaction post-CPT fails to meet the minimum specified criteria the test shall be repeated at the concerned location as directed by the Engineer. If the results of the additional testing also fail to meet the specified compliance criteria, the fills in the area shall be re-compacted and re-tested.

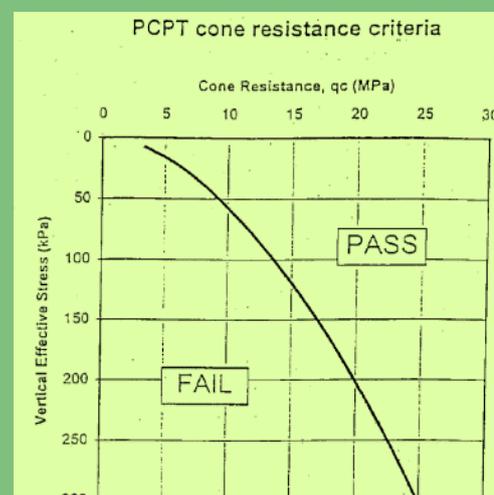


Fig. 19B The Plot for Vertical Effective Stress Vs the  $q_c$  of Post CPT for the Acceptance Criterion for Central Reclamation Project Phase III

For construction practice in Hong Kong, the deep compaction specialist contractors generally specify the limits of application for deep vibrocompaction technique based on some of the technical research and their past experiences.

In the Central Reclamation Project, Vibroflotation Group specified that fine content of soil for reclamation should not be greater than 10% and the friction ratio should not be greater than 0.8 %. Some of the projects in Asia from Keller Group generally specifies that the fine content and friction ratio should not be greater than 15% and 1% respectively.

### 4.3 Relative Density and CPT

The measurement of change in relative density ( $D_r$ ) is also commonly adopted as the quality control (QC) criterion. However,  $D_r$  does not always well link with soil behaviour especially in sandy soils with high fines content. Besides, it can vary considerably with grain mineralogy and characteristics. Current methods of using CPT measurements for QC for deep compaction often apply only to clean silica sands and are ineffective in soils with higher fines content (Robertson, 2016). There are considerable amounts of publications that demonstrate the unreliability of relative density as an acceptance criterion. The improper estimation of the sand compressibility can produce the uncertainty in the evaluated relative density up to 20%. However, it is still adopted commonly by geotechnical professionals due to its simple application.

The definition of relative density is as below:

$$D_r = \frac{e_{max} - e}{e_{max} - e_{min}} \times 100\% \quad \text{---- Equation 13}$$

$$= \frac{\gamma_{d\ max}}{\gamma_d} \times \frac{\gamma_d - \gamma_{d\ min}}{\gamma_{d\ max} - \gamma_{d\ min}} \times 100\%$$

where

- $e_{min}$  = void ratio of soil in densest condition
- $e_{max}$  = void ratio of soil in loosest condition
- $e$  = In-place void ratio
- $\gamma_{d\ max}$  = Dry unit weight of soil in densest condition
- $\gamma_{d\ min}$  = Dry unit weight of soil in loosest condition
- $\gamma_d$  = In-place dry unit weight

For clean sand less than 15 percent fines content, it is common practice to assess the relative density ( $D_r$ ) by in-situ tests. The recent re-examination of a large Calibration Chamber Test data by Jamiolkowski, et al. (2001) which incorporates a correction factor has found that a mean relationship in terms of corrected cone tip stress can be expressed by the following equation, and

the effects of relative sand compressibility can be considered by reference to Figure 20A.

$$D_R = 100 \cdot \left[ 0.268 \cdot \ln \left( \frac{q_t / \sigma_{atm}}{\sqrt{\sigma_{vo}' / \sigma_{atm}}} \right) - 0.675 \right] \quad \text{---- Equation 14}$$

where  $\sigma_{atm}$  = Pa = Atmospheric pressure  
 $D_R = D_r$

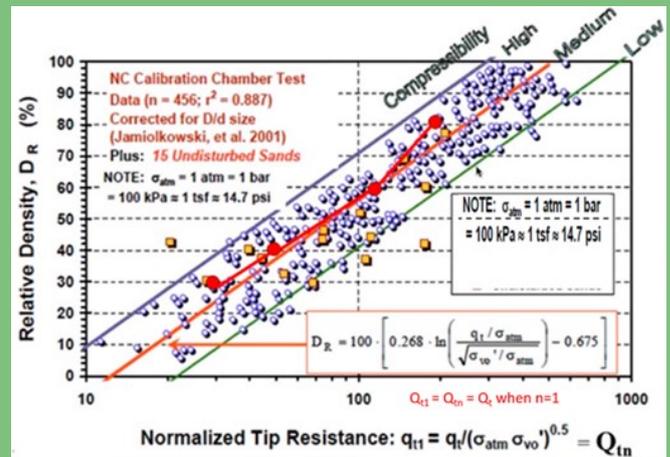


Fig. 20A Relationship Amongst Relative Density, Corrected Cone Resistance and Sand Compressibility from Corrected Chamber Test Results

One of the acceptance criteria for the performance of deep compaction works at Central Reclamation Site is based on the achievement of relative density of greater than 80% after the deep compaction work. However, it is shown in Figure 20B that part of the post treated zone at shallow depth is failed to achieve the requirement, and therefore, remedial work by means of re-compaction should be conducted.

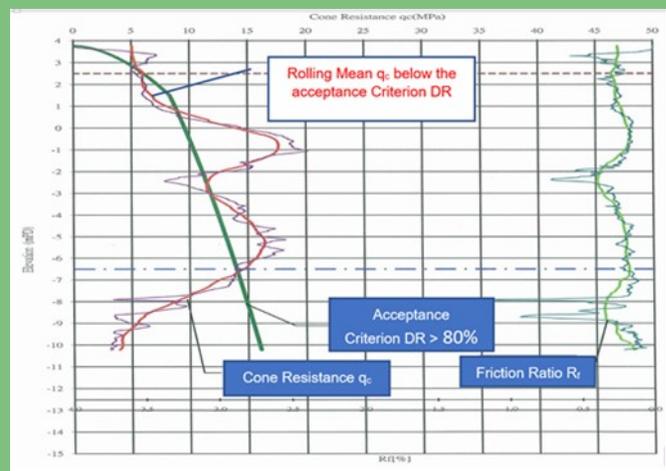


Fig. 20B Plot of Acceptance Criterion  $q_c$  at Relative Density Profile of 80% Vs Actual and Rolling Mean of Post-CPT  $q_c$  and  $R_f$  (From Central Reclamation Phase III)

#### 4.4 Change in $I_c$ for Compaction Works

The data from the site, Port of Los Angeles Phase II shows that the CPT behaviour type index  $I_c$  shifts towards a smaller number after deep compaction work. The majority of the points in Figure 21 were transformed from area 6 to 7. It seems that the soil became coarser in grain size after compaction work which of course not. The soil granulometry remains the same after vibrocompaction, and this shift of the points can be partially attributed to the increase in relative density.

$I_c$  has not been used as one of the criteria for acceptance test for the deep compaction works. As analysis of soil type behaviour using the classification charts with additional soil type behaviour index  $I_c$ , it provides better and more comprehensive approach to the soil improvement. The Figure 22 shows that the  $I_c$  values for the soil are reduced from values to lower values after the deep compaction and the improvement factors could be assessed. Therefore, it is suggested that in future vibrocompaction projects the plotting of  $q_c$  over  $I_c$  should become a routine process by which the soil compatibility can be analysed much better.

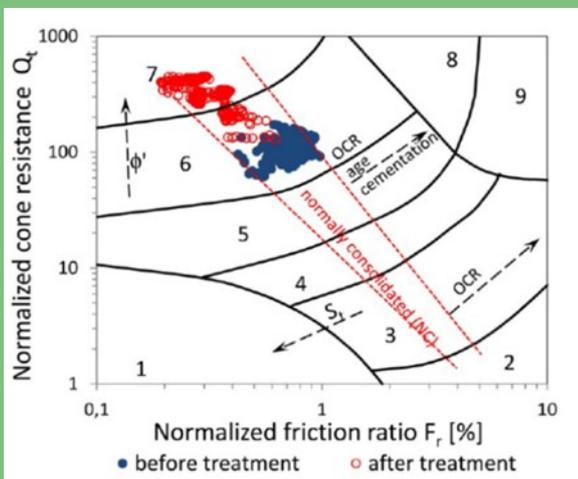


Fig. 21 Shift of  $I_c$  Before and After Deep Compaction

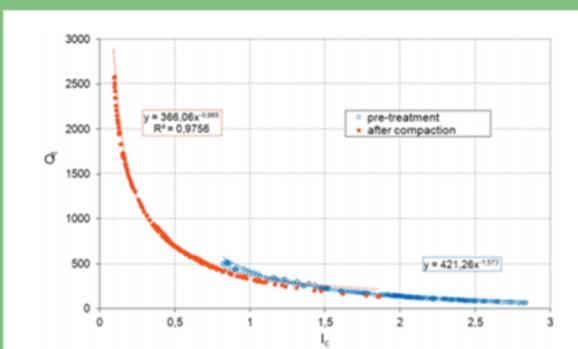


Fig. 22 Plot of Normalized Cone resistance  $Q_t$  vs Soil Behaviour Type Index  $I_c$

#### 5. Application of CPT in Deep Cement Mixing Work

##### 5.1 Calibration of CPT and Torque of A Cutter Soil Mixer

Before commencement of the deep mixing work, the  $q_t$  or  $q_c$  has been to be used to calibrate with torques and pressures at the left and right rotating soil cutting drums during a trial test with CPT penetration.

For example, a deep mixing panel record from one of the local infrastructure projects as shown in Figure 23, indicates that the two rotating drums (i.e., the cutter mixers) reached the hydraulic pressures of 280 bars and 270 bars respectively at level of -17.37mPD, and maintained the pressures of greater than 100 bars for more than 10 seconds. Since it has been calibrated before in trial, the hydraulic pressure of 100 bars from the rotating drums is equivalent to the  $q_t$  value of 1.2 MPa. The drums have sustained the hydraulic pressures which are higher than the designed top level of the competent stratum with the  $q_t$  value of 1MPa. After confirming the top level of the above competent stratum has reached with satisfaction in  $q_t$  value, the cutter mixers should further penetrate 2m to terminate level as the designed toe level of the panel.

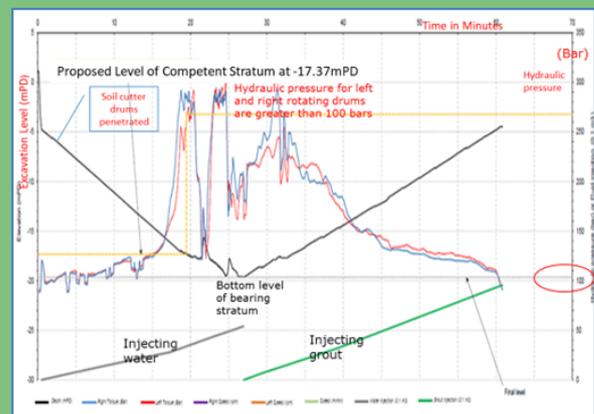


Fig. 23 Plot of Penetration of Soil Cutters in Depth with Related Hydraulic Pressures that Calibrated Before Deep Mixing Work

##### 5.2 Determination of Toe and Bottom Levels of Competent Stratum of Deep Mixing Column

The total cone resistance  $q_t$  is frequently be used in marine infrastructures in Hong Kong to determine the bearing stratum level for the marine deep mixing work. For one of the local infrastructure projects, it is specified in the contract required CPT profile ( $q_{tc}$  values), as shown as the red line profile at Figure 24, should be based on the following requirements:

1. For depth of the CPT shallower than 15m below seabed level (msbl), the corrected  $q_t$  should be greater than 1,000 KPa.
2. For depth of greater than 15msbl, the corrected  $q_t$  value should be greater than  $210+56z$  KPa, where  $z$  is the depth below the seabed level

The raw data  $q_c$  values are transformed into  $q_t$  values, and then calculated with filtering, shortening, and smoothing methods to get the  $q_{t,r}$  values (Representative CPT profile). The trial for the potential top level of the competent stratum should be checked such that  $q_{t,r}$  values should be greater than 90% of the  $q_{t,c}$  values and the  $q_{t,r}$  values should be greater than 80% of  $q_{t,c}$  along 2m below the potential top level. After that, the data should be further adjusted and assessed with several procedures specified in the appendix of the contract specification under one of the local projects to determine the top and bottom of the competent bearing stratum of a deep cement mixing column.

It should note that the raw data  $q_c$  values have been used directly to calculate and assess the competent stratum for the column in spite of approaching with correlated geotechnical parameters from CPT. For foundation design by means of using CPT values, the direct approach is commonly adopted by using the  $q_c$  and  $f_s$  to find the bearing capacity and friction of a soil stratum. One of the direct approaches, the LCPC method introduced by Bustamante and Ganeselli (1982), is commonly adopted for calculating the allowable bearing capacity for the deep foundation. It is uncommon and might be more complicated to approach through correlation of geotechnical parameters.

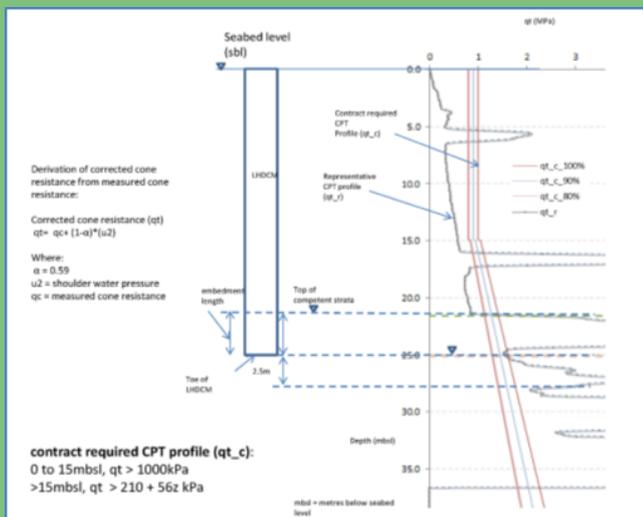


Fig. 24 Termination Criterion of CPT for Bearing Strata of A Deep Cement Mixing Project

## 6. Abbreviation and Symbols

### Standard Cone Measurements and Factors

pwp	Pore water pressure
$q_c$	Measured cone end resistance
$\alpha$	Cone shaft face to face ratio
$\beta$	value of excessive pwp cone ratio- 0.8 for the face ( $u_1$ ) and 1.0 on the shoulder ( $u_2$ )
$u_0$	Theoretical hydrostatic pwp relative to ground level acting on cone.
$u_1$	Measured pwp at cone face elevation
$u_2$	Measured pwp at cone shoulder
$u_3$	Measured pwp behind cone sleeve tube

### Pressures

$\sigma_{vo}$	Total overburden ground pressure
$\sigma_{vo}'$	Effective overburden ground pressure
$\sigma_{atm}$	Atmospheric pressure (Pa)

### SBT Soil Bar Type

$q_t$	Total cone end resistance corrected for pwp effect where $q_t = (1-\alpha) \cdot (u_0 + \beta (u_2-u_0))$
$q_n$	Net cone end resistance where $q_n = q_t - \sigma_{vo}$
$\sigma_{atm}$	Atmospheric pressure (Pa)

### Normalised Parameters

SBTn Normalized Soil Bar Type

$$Q_t = \text{Normalized cone resistance} = ((q_t - \sigma_{vo}) / \sigma_{vo}')$$

$$F_r = \text{Friction Ratio} = f_s / (q_t - \sigma_{vo})$$

$$B_q = \text{Pore Pressure Ratio} = f_s / (q_t - \sigma_{vo})$$

### Updated Normalized Parameters

$$Q_{tn} = \text{Normalized net cone resistance} = ((q_t - \sigma_{vo}) / P_a) \cdot (P_a / \sigma_{vo}')^n$$

$n$  = Stress Exponent factor where  
 $n=1$  for clay  
 $n=0.5$  for sand

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